# Chart-Based Decoding 

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Most slides courtesy of Philipp Koehn

## Overview of Syntactic Decoding



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## Syntactic Decoding

Inspired by monolingual syntactic chart parsing:
During decoding of the source sentence, a chart with translations for the $O\left(n^{2}\right)$ spans has to be filled


## Syntax Decoding



German input sentence with tree

## Syntax Decoding



Purely lexical rule: filling a span with a translation (a constituent)

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Purely lexical rule: filling a span with a translation (a constituent)

## Syntax Decoding



Complex rule: matching underlying constituent spans, and covering words

## Syntax Decoding



Complex rule with reordering

## Syntax Decoding



## Bottom-Up Decoding

- For each span, a stack of (partial) translations is maintained
- Bottom-up: a higher stack is filled, once underlying stacks are complete



## Chart Organization



- Chart consists of cells that cover contiguous spans over the input sentence
- Each cell contains a set of hypotheses
- Hypothesis $=$ translation of span with target-side constituent


## Dynamic Programming

Applying rule creates new hypothesis


## Dynamic Programming

## Another hypothesis



Both hypotheses are indistiguishable in future search $\rightarrow$ can be recombined

## Recombinable States

Recombinable?


## Recombinable States

## Recombinable?



Yes, if max. 2-gram language model is used

## Recombinability

Hypotheses have to match in

- span of input words covered
- output constituent label
- first $n-1$ output words not properly scored, since they lack context
- last $n-1$ output words
still affect scoring of subsequently added words, just like in phrase-based decoding
( $n$ is the order of the $n$-gram language model)


## Language Model Contexts

When merging hypotheses, internal language model contexts are absorbed


## Stack Pruning

- Number of hypotheses in each chart cell explodes
$\Rightarrow$ need to discard bad hypotheses e.g., keep 100 best only
- Different stacks for different output constituent labels?
- Cost estimates
- translation model cost known
- language model cost for internal words known
$\rightarrow$ estimates for initial words
- outside cost estimate? (how useful will be a NP covering input words 3-5 later on?)


## Naive Algorithm: Blow-ups

- Many subspan sequences
for all sequences $s$ of hypotheses and words in span [start,end]
- Many rules

$$
\text { for all rules } r
$$

- Checking if a rule applies not trivial rule $r$ applies to chart sequence $s$
$\Rightarrow$ Unworkable


## Solution

- Prefix tree data structure for rules
- Dotted rules
- Cube pruning


## Storing Rules

- First concern: do they apply to span?
$\rightarrow$ have to match available hypotheses and input words
- Example rule

$$
\mathrm{NP} \rightarrow \mathrm{X}_{1} \text { des } \mathrm{X}_{2} \mid \mathrm{NP}_{1} \text { of the } \mathrm{NN}_{2}
$$

- Check for applicability
- is there an initial sub-span that with a hypothesis with constituent label NP?
- is it followed by a sub-span over the word des?
- is it followed by a final sub-span with a hypothesis with label NN?
- Sequence of relevant information
$\mathrm{NP} \bullet$ des $\bullet \mathrm{NN} \bullet \mathrm{NP}_{1}$ of the $\mathrm{NN}_{2}$


## Rule Applicability Check

Trying to cover a span of six words with given rule

$$
\mathrm{NP} \bullet \text { des } \bullet \mathrm{NN} \rightarrow \mathrm{NP}: \mathrm{NP} \text { of the NN }
$$


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## Rule Applicability Check

First: check for hypotheses with output constituent label NP

$$
\mathrm{NP} \bullet \text { des • NN } \rightarrow \mathrm{NP}: \mathrm{NP} \text { of the NN }
$$


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## Rule Applicability Check

Found NP hypothesis in cell, matched first symbol of rule

$$
\mathrm{NP} \bullet \text { des } \bullet \mathrm{NN} \rightarrow \mathrm{NP}: \mathrm{NP} \text { of the NN }
$$


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## Rule Applicability Check

Matched word des, matched second symbol of rule

$$
\mathrm{NP} \bullet \text { des } \bullet \mathrm{NN} \rightarrow \mathrm{NP}: \mathrm{NP} \text { of the NN }
$$


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## Rule Applicability Check

Found a nN hypothesis in cell, matched last symbol of rule
$N P \bullet d e s \bullet N N \rightarrow N P: N P$ of the NN


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## Rule Applicability Check

Matched entire rule $\rightarrow$ apply to create a NP hypothesis
$N P \bullet$ des $\bullet N N \rightarrow N P: N P$ of the NN


## Rule Applicability Check

Look up output words to create new hypothesis (note: there may be many matching underlying NP and NN hypotheses)

## $N P \bullet$ des •NN $\rightarrow \mathrm{NP}: \mathrm{NP}$ of the NN



## Checking Rules vs. Finding Rules

- What we showed:
- given a rule
- check if and how it can be applied
- But there are too many rules (millions) to check them all
- Instead:
- given the underlying chart cells and input words
- find which rules apply


## Prefix Tree for Rules



## Highlighted Rules

$$
\begin{gathered}
\mathrm{NP} \rightarrow \mathrm{NP}_{1} \mathrm{DET}_{2} \mathrm{NN}_{3} \mid \mathrm{NP}_{1} \mathrm{IN}_{2} \mathrm{NN}_{3} \\
\mathrm{NP} \rightarrow \mathrm{NP}_{1} \mid \\
\mathrm{NP} \rightarrow \mathrm{NP}_{1} \\
\mathrm{NP} \rightarrow \mathrm{NP}_{1} \text { des } \mathrm{NN}_{2} \mid \\
\mathrm{NP} P_{1} \text { of the } \mathrm{NN}_{2} \\
\mathrm{NP} \rightarrow \mathrm{NES}_{2} \mathrm{NN}_{2}\left|\mathrm{NP}_{2} \mathrm{NP}_{1} \mathrm{NN}_{2}\right| \\
\mathrm{NET}
\end{gathered}
$$

## Dotted Rules: Key Insight

- If we can apply a rule like

$$
\mathrm{p} \rightarrow \mathrm{ABC} \mid \mathrm{x}
$$

to a span

- Then we could have applied a rule like

$$
\mathrm{q} \rightarrow \mathrm{AB} \mid \mathrm{y}
$$

to a sub-span with the same starting word
$\Rightarrow$ We can re-use rule lookup by storing A B • (dotted rule)

## Finding Applicable Rules in Prefix Tree



## Covering the First Cell



## Looking up Rules in the Prefix Tree



## Taking Note of the Dotted Rule



## Checking if Dotted Rule has Translations



## Applying the Translation Rules



## Looking up Constituent Label in Prefix Tree



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## Add to Span's List of Dotted Rules



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## Moving on to the Next Cell



## Looking up Rules in the Prefix Tree



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## Taking Note of the Dotted Rule



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## Checking if Dotted Rule has Translations



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## Applying the Translation Rules



## Looking up Constituent Label in Prefix Tree



## Add to Span's List of Dotted Rules



## More of the Same



## Moving on to the Next Cell



## Covering a Longer Span

Cannot consume multiple words at once All rules are extensions of existing dotted rules Here: only extensions of span over das possible


## Extensions of Span over das



## Looking up Rules in the Prefix Tree



## Taking Note of the Dotted Rule



## Checking if Dotted Rules have Translations



## Applying the Translation Rules



## Looking up Constituent Label in Prefix Tree



## Add to Span's List of Dotted Rules



## Even Larger Spans

Extend lists of dotted rules with cell constituent labels
span's dotted rule list (with same start) plus neighboring
span's constituent labels of hypotheses (with same end)


## Reflections

- Complexity $O\left(r n^{3}\right)$ with sentence length $n$ and size of dotted rule list $r$
- may introduce maximum size for spans that do not start at beginning
- may limit size of dotted rule list (very arbitrary)
- Does the list of dotted rules explode?
- Yes, if there are many rules with neighboring target-side non-terminals
- such rules apply in many places
- rules with words are much more restricted


## Difficult Rules

- Some rules may apply in too many ways
- Neighboring input non-terminals

$$
\mathrm{VP} \rightarrow \text { gibt } \mathrm{X}_{1} \mathrm{X}_{2} \mid \text { gives } \mathrm{NP}_{2} \text { to } \mathrm{NP}_{1}
$$

- non-terminals may match many different pairs of spans
- especially a problem for hierarchical models (no constituent label restrictions)
- may be okay for syntax-models
- Three neighboring input non-terminals $\mathrm{VP} \rightarrow \operatorname{trifft} \mathrm{X}_{1} \mathrm{X}_{2} \mathrm{X}_{3}$ heute $\mid$ meets $\mathrm{NP}_{1}$ today $\mathrm{PP}_{2} \mathrm{PP}_{3}$
- will get out of hand even for syntax models


## Where are we now?

- We know which rules apply
- We know where they apply (each non-terminal tied to a span)
- But there are still many choices
- many possible translations
- each non-terminal may match multiple hypotheses
$\rightarrow$ number choices exponential with number of non-terminals


## Rules with One Non-Terminal

Found applicable rules PP $\rightarrow$ des $\mathrm{X} \mid \ldots$ NP $\ldots$


- Non-terminal will be filled any of $h$ underlying matching hypotheses
- Choice of $t$ lexical translations
$\Rightarrow$ Complexity $O(h t)$
(note: we may not group rules by target constituent label, so a rule NP $\rightarrow$ des $\mathrm{x} \mid$ the NP would also be considered here as well)


## Rules with Two Non-Terminals

Found applicable rule NP $\rightarrow \mathrm{X}_{1}$ des $\mathrm{X}_{2} \mid \mathrm{NP}_{1} \ldots \mathrm{NP}_{2}$


- Two non-terminal will be filled any of $h$ underlying matching hypotheses each
- Choice of $t$ lexical translations
$\Rightarrow$ Complexity $O\left(h^{2} t\right)$ - a three-dimensional "cube" of choices
(note: rules may also reorder differently)


## Filling a Constituent



## Beam Search

|  | man | -3.6 | the man | -4.3 | some men | -6.3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| seen -3.8 | seen man -8.8 | seen the man | -7.6 | seen some men | -9.5 |  |
| saw -4.0 | saw man -8.3 | saw the man | -6.9 | saw some men | -8.5 |  |
| view -4.0 | view man -8.5 | view the man -8.9 | view some men -10.8 |  |  |  |

## Cube Pruning [Chiang, 2007]

man -3.6 the man -4.3 some men -6.3<br>seen -3.8 Queue<br>saw -4.0<br>view -4.0

## Queue

Hypothesis
$\rightarrow$ seen man
$-3.8-3.6=-7.4$

## Cube Pruning [Chiang, 2007]

```
man -3.6 the man -4.3 some men -6.3
seen -3.8 seen man -8.8 Queue
saw -4.0 Queue
view -4.0
```


## Queue



## Cube Pruning [Chiang, 2007]

|  | man | -3.6 | the man -4.3 | some men | -6.3 |
| :--- | :--- | ---: | :--- | :--- | :--- |
| seen -3.8 | seen man -8.8 | Queue |  |  |  |
| saw -4.0 | saw man | -8.3 | Queue |  |  |
| view -4.0 | Queue |  |  |  |  |

## Queue

| Hypothesis | Sum |
| :---: | ---: |
| $\rightarrow$ view man | $-4.0-3.6=-7.6$ |
| seen the man | $-3.8-4.3=-8.1$ |
| saw the man | $-4.0-4.3=-8.3$ |

## Cube Pruning versus Beam Search

Same Bottom-up with fixed-size beams
Different Beam filling algorithm

## Queue of Cubes

- Several groups of rules will apply to a given span
- Each of them will have a cube
- We can create a queue of cubes
$\Rightarrow$ Always pop off the most promising hypothesis, regardless of cube
- May have separate queues for different target constituent labels


## Bottom-Up Chart Decoding Algorithm

1: for all spans (bottom up) do
2: extend dotted rules
3: for all dotted rules do
4: $\quad$ find group of applicable rules
5: create a cube for it
6: create first hypothesis in cube
7: $\quad$ place cube in queue
8: end for
9: for specified number of pops do
10: pop off best hypothesis of any cube in queue
11: add it to the chart cell
12: create its neighbors
13: end for
14: extend dotted rules over constituent labels
15: end for

## Two-Stage Decoding

- First stage: decoding without a language model (-LM decoding)
- may be done exhaustively
- eliminate dead ends
- optionably prune out low scoring hypotheses
- Second stage: add language model
- limited to packed chart obtained in first stage
- Note: essentially, we do two-stage decoding for each span at a time


## Coarse-to-Fine

- Decode with increasingly complex model
- Examples
- reduced language model [Zhang and Gildea, 2008]
- reduced set of non-terminals [DeNero et al., 2009]
- language model on clustered word classes [Petrov et al., 2008]


## Outside Cost Estimation

- Which spans should be more emphasized in search?
- Initial decoding stage can provide outside cost estimates

- Use min/max language model costs to obtain admissible heuristic (or at least something that will guide search better)


## Open Questions

- Where does the best translation fall out the beam?
- Are particular types of rules too quickly discarded?
- Are there systemic problems with cube pruning?


## Summary

- Synchronous context free grammars
- Extracting rules from a syntactically parsed parallel corpus
- Bottom-up decoding
- Chart organization: dynamic programming, stacks, pruning
- Prefix tree for rules
- Dotted rules
- Cube pruning

